## Spring 2015, MATH 408, Exam 2

Monday, April 20, 2015; 12–12:50pm

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Name: \_

## ${\rm Circle\ the\ time\ of\ your\ discussion\ section:}\quad 8am \quad 9am \quad 10am$

## Instructions:

- No books or notes of any kind.
- Turn off cell phones.
- You should have (and use!) a calculator and three distribution tables: normal, t, and  $\chi^2$ .
- Answer all questions and clearly indicate your answers.
- Each problem is worth 10 points.
- Show your work! Points might be taken off for a correct answer with no explanations. Wrong answer with no explanations is worth zero points.

Problem	Possible	Actual
1	10	
2	10	
3	10	
4	10	
5	10	
Total	50	

 $\mathbf{2}$ 

Problem 1. Consider the one-way layout model in the form

 $Y_{ij} = \theta_i + \varepsilon_{ij}, \quad \varepsilon_{ij} \text{ are iid } \mathcal{N}(0, \sigma^2), \quad i = 1, \dots, k, \quad j = 1, \dots, n.$ 

Describe the test statistic and the rejection region for testing the null hypothesis

$$H_0: \theta_1 = \theta_2 = \cdots = \theta_k$$

against the alternative that  $\theta_p \neq \theta_q$  for at least one pair  $(p,q), p \neq q$ .

Problem 2. Consider the model in the form

 $Y_{ij} = \theta_i + \mu_j + \varepsilon_{ij}, \quad \varepsilon_{ij} \text{ are iid } \mathcal{N}(0, \sigma^2), \quad i = 1, \dots, k, \quad j = 1, \dots, n.$ Describe the test statistic and the rejection region for testing the null hypothesis

$$H_0: \theta_1 = \theta_2 = \cdots = \theta_k$$

against the alternative that  $\theta_p \neq \theta_q$  for at least one pair  $(p,q), p \neq q$ .

**Problem 3.** To test whether a die is fair, 66 rolls were made, and the corresponding outcomes were as follows:

Fac	e value	Observed frequency	
	1	7	
	2	9	
	3	17	
	4	16	
	5	9	
	6	8	

Estimate the P-value if the  $\chi^2$  test is used.

**Problem 4**. In a certain city, there are about one million eligible voters. To study the relationship between sex and participation in the last election, a simple random sample of size 10,000 was chosen. The results:

	Men	Women
Voted	2,850	$3,\!550$
Didn't vote	$1,\!450$	$2,\!150$

Compute the P-values for the  $\chi^2$ -test of the null hypothesis that sex and voting are independent.

**Problems 5.** A coin-making machine produces pennies in such a way that, for each coin, the probability U to turn up heads is uniform on [0, 1]. A coin pops out of the machine. Compute the conditional distribution of U given that the coin is flipped 1000 times and lands heads 300 times.