May 6, 2013 KAP 414 2:15 PM- 3:15 PM

Prof. Nizar Touzi

(Ecole Polytechnique)

"Martingale optimal transport and model-free hedging"

Abstract: The martingale optimal transportation problem is motivated by model-independent bounds for exotic options in financial mathematics. In this talk, we extend the one-dimensional Brenier's theorem to the present martingale version. We provide the explicit martingale optimal transference plans for a remarkable class of coupling functions corresponding to the lower and upper bounds. Our approach relies heavily on the (weak) duality result, and provides, as a by-product, an explicit expression for the corresponding optimal semi-static hedging strategies. Using the extension to the multiple marginals case, we also provide the analogous result in continuous-time. In particular, the continuous-time limit provides a remarkable PCOC process, namely a pure jump martingale local Levy process with prescribed marginals.