Photoexcited Nonadiabatic Dynamics of Solvated Push–Pull \( \pi \)-Conjugated Oligomers with the NEXMD Software

Andrew E. Sifain, Josiah A. Bjorgaard, Tammie R. Nelson, Benjamin T. Nebgen, Alexander J. White, Brendan J. Gifford, David W. Gao, Oleg V. Prezhdo, Sebastian Fernandez-Alberti, Adrian E. Roitberg, and Sergei Tretiak

1Department of Physics and Astronomy and 5Department of Chemistry, University of Southern California, Los Angeles, California 90089, United States
2Theoretical Division, 6Center for Nonlinear Studies, 7Computational Physics Division, and 8Center for Integrated Nanotechnologies, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, United States
6Department of Chemistry and Biochemistry, North Dakota State University, Fargo, North Dakota 58108, United States
8Los Alamos High School, Los Alamos, New Mexico 87544, United States
9Universidad Nacional de Quilmes/CONICET, Roque Saenz Peña 352, B1876BXD Bernal, Argentina
◆Department of Chemistry, University of Florida, Gainesville, Florida 32611, United States

ABSTRACT: Solvation can be modeled implicitly by embedding the solute in a dielectric cavity. This approach models the induced surface charge density at the solute–solvent boundary, giving rise to extra Coulombic interactions. Herein, the Nonadiabatic EXcited-state Molecular Dynamics (NEXMD) software was used to model the photoexcited nonradiative relaxation dynamics in a set of substituted donor–acceptor oligo(p-phenylenevinylene) (PPVO) derivatives in the presence of implicit solvent. Several properties of interest including optical spectra, excited state lifetimes, exciton localization, excited state dipole moments, and structural relaxation are calculated to elucidate dependence of functionalization and solvent polarity on photoinduced nonadiabatic dynamics. Results show that solvation generally affects these properties, where the magnitude of these effects varies from one system to another depending on donor–acceptor substituents and molecular polarizability. We conclude that implicit solvation can be directly incorporated into nonadiabatic simulations within the NEXMD framework with little computational overhead and that it qualitatively reproduces solvent-dependent effects observed in solution-based spectroscopic experiments.

1. INTRODUCTION

Modeling nonadiabatic excited state molecular dynamics is at the core of understanding photoinduced processes such as charge and energy transfer,\(^{1-4}\) photoisomerization,\(^{7,8}\) photodissociation,\(^{9,10}\) and other types of coupled electron–vibrational (or vibronic) dynamics.\(^{11-13}\) In organic conjugated molecules, photoinduced relaxation occurs in a dense manifold of vibrational and electronic states due to strong electronic correlations and electron–phonon couplings.\(^{14-16}\) A theoretical understanding of excited state relaxation in these materials not only aids in the design of functional photocative materials for technological applications,\(^{17-24}\) but also elucidates photochemical and photophysical properties that frequently go undetected in experiments such as conformational changes, multiple reaction pathways, and electron density distributions.\(^{25,26}\) Our ability to gain understanding at the molecular level is largely dictated by the reliability of computational methods. Due to the large number of degrees of freedom in a solvent, nonadiabatic simulations of realistically large molecular systems (tens to hundreds of atoms in size) are typically performed in the gas phase, whereas most experiments are carried out by probing solution-based or solid-state samples. The use of qualitatively accurate and numerically efficient methods of modeling solvation is necessary for predicting and interpreting structural, optical, and dynamical properties. Herein, we implement a solvent model in the Nonadiabatic EXcited-state Molecular Dynamics (NEXMD) software and demonstrate its effects on the photoinduced nonadiabatic dynamics in a set of organic conjugated push–pull (or donor–acceptor) molecules.

The solute–solvent system is most accurately modeled by quantum mechanics. However, this approach is prohibitively expensive for systems with multiple degrees of freedom.

Received: January 31, 2018
Published: June 6, 2018

DOI: 10.1021/acs.jctc.8b00103
Therefore, approximations capable of reproducing the effective solvent response in large systems are needed. One such method resorts the portion of solvent interacting with the solute to a quantum mechanical description using a combined quantum mechanical/molecular mechanical (QM/MM) approach.27-29 At this level, the ab initio molecular dynamics would still require averaging over many solvent configurations.30-32

Implicit solvent models reduce computational cost even further by treating the solvent as a dielectric continuum—an effective average over many solvent configurations.33-37 By embedding the solute in a dielectric cavity,38 charge density of the solute induces a surface charge density in the cavity, producing a polarization that screens Coulombic interactions. Analytical gradients in time-dependent density functional theory (TD-DFT) and time-dependent Hartree–Fock (TD-HF) make it feasible to include solvent effects at the first-order or linear response level.39-41 In this way, the solvent responds linearly to the excitation of the solute which is determined by the spatial distribution of the transition density.40,41

The NEXMD software uses semiempirical Hamiltonians within TD-HF theory, thereby making it feasible to implement a linear response solvent model.40,41 The use of semiempirical Hamiltonians allows NEXMD to simulate the dynamics of organic conjugated molecules on the order of hundreds of atoms and for time scales up to tens of picoseconds. Past developmental versions of NEXMD have been used to simulate the nonadiabatic dynamics of large systems such as dendrimers,42-45 chlorophylls,46-48 cycloparaphenylenes,49 and conjugated macrocycles.5 Integrating an implicit solvent model to the code is both an efficient way to model large systems with dense manifolds of interacting excited states and may be computed as evidenced by successful application of this level of theory to systems such as polymers,44,45,51-53 dendrimers,53 light-harvesting complexes,52 and carbon nanotubes.64,65

Energies and forces as well as nonadiabatic couplings are computed “on the fly” with nuclei evolving on native excited state PESs. Nonadiabatic transitions between electronic states are modeled with Tully’s fewest-switches surface hopping (FSSH).66 Other practical aspects of calculations that are carried out with NEXMD include but are not limited to (1) decoherence corrections built on top of FSSH to alleviate inconsistencies due to the classical treatment of nuclei,67,68 (2) advanced algorithms for tracking trivial (unavoided) crossings between noninteracting states,69 (3) implicit treatment of solvation including linear response,40,41 state-specific,40,41 and nonequilibrium models,70 and (4) “on-the-fly” limiting to essential excited states that are needed to sufficiently propagate the electronic Schrödinger equation.71 The latter functionality significantly reduces computational time by eliminating the calculation of unnecessary excited states and nonadiabatic couplings. More detail on the governing theory that is implemented in developmental versions of NEXMD can be found in refs 15 and 16. Full description of the NEXMD software such as structure, use, and benchmarks will be reported elsewhere, along with a public release of the code.

For the purposes of this paper, we focus on NEXMD’s functionality of modeling implicit solvation—specifically, linear response solvation following the theoretical formalism reported in ref 40. Dynamics are coupled to the conductor-like polarizable continuum model (CPCM) from the SQM code using a standard tessellation scheme for cavity discretization.52,72 Solvent response is related to the induced polarization with coefficient given by \( f(e) = (e - 1)/e \), where \( e \) is the dielectric constant of the solvent.72,73 The surface charge distribution at the solute–solvent boundary produces an electrostatic potential which is added to the solute’s Hamiltonian. This term accounts for the interaction of the solute’s electrons and nuclei with the induced polarization charge. In order to properly simulate nonadiabatic dynamics, solvent effects are also included in the derivative coupling vectors:

\[
\mathbf{d}_{\alpha\beta} = \frac{\langle \phi_{\alpha}(\mathbf{r}; \mathbf{R}) | \nabla_{\mathbf{R}} H | \phi_{\beta}(\mathbf{r}; \mathbf{R}) \rangle}{E_{\beta} - E_{\alpha}}
\]

where \( H \) is the electronic Hamiltonian, parametrized by nuclear configuration, and contains a term for the solute–solvent interaction: \( H = H_{\text{elc}} + H_{\text{int}} \). The adiabatic eigenvectors and eigenvalues of \( H \) are \( |\phi\rangle \) and \( E \), respectively.

CPCM approximates PCM and treats the solvent as a conductor which simplifies numerical integration of Poisson’s equation at the solute–solvent boundary. The coefficient of polarization \( f(e) \) is an artificial function that ensures modeling of a solvent with a finite dielectric constant as opposed to a perfect conductor with an infinite dielectric constant. Nevertheless, CPCM has successfully reproduced experimental results.75

2.2. Studied PPVO Derivatives. \( p \)-Phenylenvinylene (PPV) is a prototype conjugated polymer with potential use in optoelectronic devices due to its rich electronic and optical properties as well as synthetic flexibility.74-84 The PPVO derivatives (Figure 1) are molecular chromophores with large systems with dense manifolds of interacting excited states
tunable emission energies ranging across the optical spectrum.\(^8^5^,8^6\) In our simulations, we use the following three oligomers: unsubstituted \{H, H\}, substitution with an acceptor \{H, NO\}_2\}, and substitution with a donor—acceptor \{NH\}_2\ NO\}_2\}. These molecules can adapt two distinct asymmetric and symmetric conformations as illustrated in Figure 1, parts A and B, respectively.

These molecules were chosen mainly because of their varying degrees of polarizability as a result of chemical substitution.\(^8^7\)

The calculated ground state dipole moments \(\vec{\mu}_{\text{gg}}\) vary between 1.5−2.0, 6.8−7.9, and 8.4−9.6 D in \{H, H\}, \{H, NO\}_2\}, and \{NH\}_2\ NO\}_2\}, respectively. The lower and upper bounds of each range correspond to \(\vec{\mu}_{\text{gg}}\) with \(\epsilon = 1\) and \(\epsilon = 20\), respectively. The dipole moment progressively increases from apolar to polar molecules. Thus, we expect to see differences in the calculated excited state properties due to differences in their respective solute–solvent interactions.

2.3. Nonadiabatic Dynamics Simulations. The protocol taken to model nonadiabatic dynamics have been reported,\(^1^6\) but for the sake of completeness, we summarize the steps here as well. A more detailed procedure is available in the Supporting Information. All molecular geometries were optimized using AM1 in NEXMD and then evolved adiabatically on their respective ground states for several nanoseconds with a 0.50 fs time step in a Langevin thermostat set to 300 K and a friction parameter of 20 ps\(^−^1\). Snapshots were taken throughout the equilibrated ground state trajectories of both conformers (Figure 1) which constitute inputs to excited state modeling. In our simulations, 80% of initial geometries used for nonadiabatic trajectories were sampled from the ground state trajectories of the asymmetric conformations of Figure 1A, while the other 20% were sampled from the other ground state trajectories with the symmetric conformations of Figure 1B. These proportions are approximate Boltzmann populations determined from total energies of the ground state optimized structures. Absolute energy differences between the ground state optimized asymmetric and symmetric conformations of these molecules using the AM1 Hamiltonian range from 0.045 to 0.063 eV. For the sake of simplicity, we used the same proportions of asymmetric (80%) and symmetric (20%) conformations for the dynamical ensembles of the three PPVO molecules.

Single-point calculations at ground state geometries were performed to determine excited state energies and oscillator strengths. Oscillator strengths were broadened with a Gaussian-shaped Franck–Condon window at the excitation energies with an empirical standard deviation of 0.15 eV. A theoretical absorption spectrum of each molecule was then calculated as an average over all the individual absorption spectra of its sampled ground state conformations. Emission spectra were also simulated to calculate Stokes shifts and compare them to experimental data. Similar to the procedure carried out for absorption, a single trajectory for each molecule evolved adiabatically on the first excited state \(S_1\) for a few nanoseconds. Following thermal equilibration, geometries were sampled throughout these trajectories and single-point calculations determined \(S_1 \rightarrow S_0\) emission energies and oscillator strengths.

Ground state snapshots (i.e., coordinates and velocities) were used as the initial conditions for nonadiabatic trajectories. Each trajectory was prepared in an optically allowed electronic excited state in the vicinity of the chosen photoexcitation energy. The initial excited state of each trajectory was chosen according to the absorption spectrum of its sampled ground state geometry such that states with larger oscillator strengths were more populated than those with lower oscillator strengths. This procedure composes a photoexcited wave packet sampling the phase space of nuclear configurations accessible at room temperature. Nonadiabatic trajectories evolved for 1 ps in length with a 0.10 fs classical time step (nuclei) and a 0.02 fs quantum time step (electrons) in the same Langevin thermostat as the ground state trajectories. Whenever FSSH signaled for a hop to occur, the electronic wave function was instantaneously collapsed onto the target state following the transition, thereby incorporating the appropriate decoherence correction.\(^8^7\) Trivial crossings were also accounted for using a method developed and tested within the NEXMD framework.\(^8^9\) In order to guarantee statistical convergence, each ensemble was comprised of 635 trajectories. A range of solvents from low to high polarity were modeled with \(\epsilon = 1, 2, 5, 20\).

2.4. Natural Transition Orbitals (NTOs) and Transition Density (TD) Analysis. Excitonic states of these \(\pi\)-conjugated oligomers have strong multireference character. Due to strong mixing, visualizing these excitations in terms of molecular orbitals does not provide useful information. A more useful analysis of the excited states was carried out by transforming molecular orbitals to natural transition orbitals (NTOs). By generating NTOs, the hole and electron wave functions were visualized and the ground to excited state transition characters were more accurately assigned as \(\pi \rightarrow \pi^*\), charge transfer, etc. These holes and electrons come in pairs, where the relative weight of each pair are excitation amplitudes in the NTO basis. NTOs were calculated in the Gaussian 09\(^9^8\) software, and images showing NTOs were obtained with the Visual Molecular Dynamics (VMD) software.

Evolution of the excitonic wave function was tracked by changes in the spatial localization of the transition density (TD). Diagonal elements of the single-electron TD matrices

\[
(p^{\rho^{\pi^*}})_{mm}(t) \equiv \langle \rho(t) \rangle_{\pi^*} c^*_m c_m \phi^{\pi^*}_m(t)
\]

represent changes in the electronic density in an atomic orbital (AO) when undergoing a ground (\(g\)) to excited state (\(e\)) transition, where \(c^*_m\) and \(c_m\) are Fermi creation and annihilation
operators, respectively; $m$ refers to the AO basis function.\textsuperscript{90} Evolution of a TD matrix contains information regarding charge density fluctuations and spatial localization of excitations in time.\textsuperscript{43,69,91,92} The fraction of TD localized on a molecular fragment is defined as the sum of all its atomic contributions.\textsuperscript{93} For the purposes of this study, each molecule was divided into two fragments and the normalized probability distribution of the TD on each fragment ($\xi$) was calculated using

$$
\xi = \frac{\sum_{n}^{(N_f)} |\xi_n|}{\sum_{j}^{(N)} |\xi_j|} \tag{3}
$$

where $\xi_n$ is TD on the $n$th atom, $\{N_f\}$ are the atoms associated with the $F$ fragment, and $\{N\}$ are all atoms of the molecule.\textsuperscript{51} $\xi$ is a $N \times N$ reduced TD matrix where diagonal elements $\xi_{nn}$ are determined by summing the contributions of TD ($\mu_{nm}$ of eq 2) from all AO basis functions associated with the $n$th atom.

In addition to describing the spatial localization of excitations with $\xi$, we also measure exciton localization $L_D$. The latter is defined as the inverse participation ratio associated with the distribution of populations\textsuperscript{51}

$$
L_D = \left\{ \sum_{n}^{N_f} p_n^2 \right\}^{-1} \tag{4a}
$$

$$
p_n = \frac{|\xi_n|^2}{\sum_j^{(N)} |\xi_j|^2} \tag{4b}
$$

For a localized excitation, $L_D \sim 1$, and for a delocalized excitation, $L_D \sim N$. Calculating $L_D$ is a simple way of determining the localization/delocalization of molecular excitations as a function of chemical substitution and solvent polarity.

### 3. RESULTS AND DISCUSSION

#### 3.1. Optical Spectra and Initial Excitation

The first step to modeling photoinduced dynamics is photoexcitation into optically allowed electronic states. The left panels of Figure 2 show the calculated absorption spectra of the three molecules with $\epsilon = 1$, where contributions of the individual excited states ($S_i - S_9$) are delineated. Three peaks are predicted within the optical window of interest, the locations of which do not vary by more than 0.20 eV across the three molecules. The right panels of Figure 2 show the integral spectrum of each molecule in four solvent environments. The spectra shift toward lower energy as $\epsilon$ increases due to stabilization of the excited states relative to the ground state caused by the induced polarization (solvatochromic shifts). These shifts are within 0.30 eV. In order to study nonadiabatic dynamics through multiple excited states, the molecules were photoexcited at the high-energy peak. The laser excitation energy was a Gaussian-shaped pulse in the energy domain with a mean of 4.30 eV and an empirical line width parameter (standard deviation) of 0.15 eV (Figure 2).

A calculated absorption spectrum was compared to an experimental spectrum from the literature in order to support the use of NEXMD’s level of theory for calculating excited states. The calculated spectrum of \{H, H\} is red-shifted relative to the experimental spectrum of PPV\textsuperscript{394} by about 0.20 eV, but the Stokes shift (which is approximately 0.5 eV) is in excellent agreement (Figure S1). This comparison between \{H, H\} and PPV3 is valid since the methoxy groups connected to the central benzene ring do not contribute to the optical excitation based on NTO analysis (discussed below). While the absolute excitation energies are slightly red-shifted compared to experiment, relative energy given by the Stokes shift is described well at the semiempirical level of theory. Similarly, nonradiative relaxation also depends on energy gaps, and therefore these results give us confidence in using NEXMD for studying qualitative differences in the dynamics due to functionalization and solvent polarity.
The molecules of this study have different partial charge transfer character and are a test bed for investigating the effects of functionalization in different solvent environments. Transitions are independent of molecular conformations across all ground state dynamical data, and therefore we only present NTOs of S1 (Table S1) and the optically excited state (Table S2) of the three molecules in their ground state optimized geometries with $\epsilon = 1$. For $\{H, H\}$, the transition to the optically excited state has $\pi \rightarrow \pi^*$ character localized on the aromatic rings. Similar $\pi \rightarrow \pi^*$ transitions occur in $\{H, NO_2\}$, but unlike $\{H, H\}$ which is an unsubstituted symmetric molecule, $\{H, NO_2\}$ favors charge transfer toward the NO$_2$. Similarly, $\{NH_2, NO_2\}$ also shows significant charge transfer from NH$_2$ to NO$_2$. The main transitions in all molecules are $\pi \rightarrow \pi^*$, but NTOs illustrate how charge transfer character can be controlled by chemical substitution. This is also reflected in the difference of dipole moments in the ground and excited states $(\mu_{ee} - \mu_{gg})$ which progressively increases from the apolar to polar molecules and varies from approximately 0.4, to 1.1, to 2.4 D across all dynamical simulations with $\epsilon = 1$. The excited states used to calculate $\mu_{ee}$ are those that contribute most to the absorption peaks at 4.30 eV, which are $S_7$ for $\{H, H\}$ and $S_9$ for $\{H, NO_2\}$ and $\{NH_2, NO_2\}$ (Figure 2).

### 3.2. Potential Energy Surfaces

Excited state dynamics depend on the topology of potential energy surfaces (PESs). Figure 3 shows solvatochromic shifts when PESs are histogrammed over all time steps and trajectories. To show relative differences in excited state energies as a function of $\epsilon$, the PESs of each molecule were shifted by their mean ground state energies with $\epsilon = 1$. As a consequence of the electrostatic interaction at the solute–solute boundary, these shifts increase in the order $\{H, H\}$, $\{H, NO_2\}$, and $\{NH_2, NO_2\}$. For $\{H, H\}$, $(E_j(\epsilon) - E_j(\epsilon=1)) = 2.79$ at $\epsilon = 1$ and 2.29 at $\epsilon = 20$, resulting in an overall shift of 0.50 eV. For $\{H, NO_2\}$ and $\{NH_2, NO_2\}$, these shifts are $2.56 - 1.80 = 0.76$ eV and $2.54 - 1.59 = 0.95$ eV, respectively. Increasing solvent polarity stabilizes the energy levels and the degree of stabilization depends on donor–acceptor groups, where more polar molecules (i.e., $\{H, NO_2\}$ and $\{NH_2, NO_2\}$) are further stabilized in more polar solvents.

### 3.3. Excited State Populations and Lifetimes

Figure 4 shows the lifetimes of electronic excitations. The initial excitation (black curve) fully decays in about 500 fs and rapidly transfers population through the intermediate states. The $S_1$ population was fitted to the expression $A - B \exp(-kt)$, where $k$ is the relaxation rate and $t$ is time (Figure 4D). Relaxation rates of $\{H, H\}$ do not strongly depend on solvent polarity since the molecule is weakly polarizable. In contrast, relaxation rates of the polar molecules do depend on solvent polarity.

Relaxation dynamics to $S_1$ are described by the energy gaps between excited states, $E_j = E_j - E_i$. The gaps of $\{H, NO_2\}$ and $\{NH_2, NO_2\}$ (Figure 3); nonadiabatic couplings$^{95}$ (eq 1) are larger in the polar molecules, leading to faster relaxation (Figure 4D). In regards to changes due to solvent polarity, energy gaps can either increase or decrease (Figure S2). [The number of gaps that fell below 0.1 eV was recorded (Figure S3). This value was chosen because the majority of hops occurred below this threshold.]

The frequency of small energy gaps in $\{H, NO_2\}$ generally
decreases with $\epsilon$, thus explaining the monotonic decrease in $k$ (Figure 4D). In contrast, the $E_{32}$ gap of \{H, NO$_2$\} decreases with increasing $\epsilon$, and explains the decrease in S$_3$’s population in more polar solvents (Figure 4A). The $S_3 \rightarrow S_2$ transition becomes more easily accessible. The $E_{98}$ gap of \{NH$_2$, NO$_2$\} fluctuates non-monotonically with $\epsilon$ (Figure S3) and correlates to changes seen in the $S_1$ population (Figure 4D). All these examples are given to highlight the effect of solvation on

Figure 4. Excited state populations of (A) \{H, H\}, (B) \{H, NO$_2$\}, and (C) \{NH$_2$, NO$_2$\}, respectively. Each subpanel of (A)–(C) shows excited state populations in one of the solvent environments with $\epsilon = \{1, 2, 5, 20\}$. Populations labeled with $S_m$ are comprised of all states that are excited by the initial laser excitation at 4.30 eV. (D) Relaxation rates to $S_1$ determined by fitting $S_1$ populations to $A - B \exp(-kt)$. Error bars are ± one standard deviation in the associated fit.

Figure 5. Fraction of transition density (TD) on specified (boxed) molecular fragments as a function of time. Asymmetric conformations of the molecules are shown for visualization, but the TDs of asymmetric and symmetric conformations are contained in the averaged results.
relaxation as a result of changes in energy gaps. The degree to which an excited state is affected by solvation depends on its polarizability and charge transfer character (discussed in section 3.5). In summary, we find that relaxation to $S_1$ occurs on a $590 - 730, 140 - 350, \text{and } 230 - 370$ fs time scale ($k^{-1}$) in {H, H}, {H, NO$_2$}, and {NH$_2$, NO$_2$}, respectively (Table S3). The range of each time scale refers to the effect of the different solvent environments.

3.4. Transition Density (TD) Analysis. Evolution of the excitonic wave function was qualitatively tracked by changes in spatial localization of the TD. Each molecule was split into two fragments, and the fraction of TD on each fragment was calculated with eq 3. In {H, H}, the excitation is split evenly on both fragments throughout the dynamics and is roughly independent of $\epsilon$ (Figure 5A). Both properties are expected since the molecule is symmetric and lacks electron donating and withdrawing groups. In {H, NO$_2$} at $\epsilon = 1$, the excitation starts out evenly distributed and then transfers toward the NO$_2$ (Figure 5B); the exciton becomes more localized as trajectories evolve due to the electron withdrawing character of NO$_2$ by induction and resonance. In {NH$_2$, NO$_2$}, the excitation slightly favors the NH$_2$ fragment at initial time (Figure 5C), in agreement with NTOs of the optically excited state (Table S2). The excitation transfers toward the NO$_2$ and the fraction transferred decreases as $\epsilon$ increases similar to that observed in {H, NO$_2$} (Figure 5B), but to a lesser extent.

The spatial distribution of the TD is a consequence of the electron withdrawing or donating character of the functional groups. Both of the polar molecules are functionalized with NO$_2$, but the fraction of TD localized on the fragment containing NO$_2$ is larger in {H, NO$_2$} than in {NH$_2$, NO$_2$} (Figure 5). The NO$_2$ group decreases electron density on the ring through an electron withdrawing effect. This effect occurs in both molecules, but in the case of {NH$_2$, NO$_2$}, the NH$_2$ group also increases electron density on the adjacent aromatic ring through an electron donating effect. As a result, the excitation is more delocalized in {NH$_2$, NO$_2$}.

In regards to trends observed due to solvent polarity, the TD on each fragment of both molecules becomes more like the other as $\epsilon$ increases, resulting in a more delocalized ground to excited state transition. This effect is a consequence of functionalization along the major inertial axis, giving rise to relatively large dipole moments. But since dipole moments are large, an increase in $\epsilon$ only slightly affects the distribution of charge density and the fraction of TD on each fragment (Figure 5). This is more so the case for {NH$_2$, NO$_2$} than it is for {H, NO$_2$}.

A brief discussion of TD as a function of individual excited states and solvent polarities is available in Supporting Information (Figure S4).

3.5. Excited State Dipole Moments. Figure 6 shows histograms of excited state dipole moments. The dipoles of {H, H} are smaller in magnitude than those of {H, NO$_2$} and {NH$_2$, NO$_2$}. The relative direction also changes from being along the minor inertial axis (Figure 6A) in the apolar molecule (Figure 6B) to being nearly parallel along the major inertial axis in the polar molecules (Figure 6C,D) as a result of chemical substitution. Dipole magnitudes increase as $\epsilon$ increases and vary...
in the ranges 1.5–2.1, 8.4–9.6, and 10.6–12.5 D in the three molecules, respectively. The dipole moments of \{H, NO₂\} and \{NH₂, NO₂\} also show small changes in magnitude within the first 200 fs, indicative of charge transfer character (Figure S5). A brief discussion on charge transfer states is available in the Supporting Information (Figure S6).

Dipole moments computed with NEXMD can be validated by considering the inertial axis along which they are oriented. Dipoles vary from approximately 2 D in \{H, H\} to 12 D in \{NH₂, NO₂\}; a ratio of 6 is in approximate agreement with the length scales of the major and minor inertial axes for these molecules.

3.6. Exciton Localization. A measure of exciton localization brings together the preceding analyses of TDs and excited state dipole moments. Figure 7 shows a scatter plot of dipole moment versus exciton localization (eq 4a) across all molecules and solvent polarities. The dipole moment of \{H, H\} is inversely related to \(L_D\) (shown in blue); an increase of the dipole moment along the minor inertial axis (Figure 6B) localizes the exciton, but only to a small extent due to the molecule’s low degree of polarizability. Once \(\epsilon > 5\), \(L_D\) saturates, thus defining a lower bound within this set of molecules. In the cases of \{H, NO₂\} and \{NH₂, NO₂\}, the excitation is more delocalized since functionalization and dipole moments are aligned along the major inertial axis. For \{H, NO₂\}, \(L_D\) gradually increases with \(\epsilon\), suggesting that the spatial extent of the excitation is more variable as a function of solvent polarity (shown in green). This is not the case for \{NH₂, NO₂\}, which experiences an upper bound on \(L_D\) at \(\epsilon > 5\) (shown in red); substitution with donor—acceptor groups attached at the ends of the molecule delocalizes the excitation so that even a small increase in \(\epsilon\) maximizes the size of the exciton. \(L_D^{\text{upper}} - L_D^{\text{lower}}\) is relatively small in these molecules (as it should be for small \(\pi\)-conjugated structures), but this analysis uncovers qualitative differences among the excitations due to functionalization and solvent polarity.

There is a connection between the results of Figure 7 and relaxation time scales of Figure 4D. Although \{NH₂, NO₂\} is more polar than \{H, NO₂\}, its exciton size does not vary as much with \(\epsilon\). Similarly, relaxation time scales of \{NH₂, NO₂\} are less dependent on solvent polarity compared to \{H, NO₂\}. In other words, the relaxation rate of the more polar molecule \{NH₂, NO₂\} is less affected by the presence of more polar solvents since its exciton size is already close to maximum. In the opposite direction, \{H, H\} is the least polar molecule; exciton size and relaxation time scales are changed only slightly due to the presence of more polar solvents. The simulations of this paper use implicit solvation, and therefore more work is needed to study this effect in the context of explicit solvation.

3.7. Bond Length Alternation (BLA). Bond length alternation (BLA) between adjacent carbon—carbon atoms, \(\left[(b_\text{H} + b_\text{D})/2\right] - b_\text{D}\) (Figure 1A), was calculated to quantify the dependence of chemical substitution and solvent polarity on structural relaxation. BLAs were calculated between both outer aromatic rings and the central ring independently (Figure 8).

BLA decreases in time, thus verifying that it is greater in the ground state than in the excited state.\(^{14,15}\) As expected, BLA does not vary as a function of solvent polarity in the apolar molecule, but does in the polar molecules. The varying dependence of BLA with solvent polarity is a consequence of zwitterions.\(^{96}\) In \{H, NO₂\}, BLA decreases with increasing \(\epsilon\) on the side containing NO₂. A zwitterion of \{H, NO₂\} shows bond order on the NO₂ side changing from single to double bond character and vice versa (Figure S7). For the same structure, bond character on the H side is unaffected, in agreement with calculations (middle left panel of Figure 8). In contrast, as a result of a zwitterion that flips bond character throughout the entire molecule (Figure S7), BLA of \{NH₂, NO₂\} decreases with increasing \(\epsilon\) on both sides of the molecule (bottom panels of Figure 8). BLA is further reduced on the side containing NH₂ which is likely due to another zwitterion that exclusively flips bond order on the NH₂ fragment, leaving the NO₂ fragment unchanged (Figure S7).

BLA decreases as \(\epsilon\) increases due to more solvent-stable resonance structures (zwitterions), where the contributions of single and double bond character become more alike. This is not the case for \{H, H\} since it lacks functional groups that can change the bond order of the adjacent carbon—carbon atoms. Both observations qualitatively agree with simple chemical expectations. This analysis not only conveys the dependence of chemical substitution and solvent polarity on structural relaxation but further validates calculations carried out with NEXMD.

3.8. Relative Computational Time. The linear response solvent model added very little computational overhead to the

Figure 7. Excited state dipole moment versus exciton localization \(L_D\). Each data point was computed as an average over all time steps and trajectories in the nonadiabatic ensembles.

Figure 8. Bond length alternation (BLA) as a function of time. Each row represents a different molecule. The left and right panels show the BLA on the side of the molecule containing \(R_1\) and \(R_2\), respectively. Coherent oscillations in the BLA are observed within the first 100 fs, which shows the transfer of optical energy to nuclear vibrational modes and the ultrafast relaxation on the femtosecond time scale.
nonadiabatic simulations. CPU times were averaged over all trajectories of each ensemble computed with and without the solvent model at \(\varepsilon = 20\) and \(\varepsilon = 1\), respectively (Figure S8). [CPU times do not vary among simulations with \(\varepsilon \neq 1\).] The total CPU time increased by slightly less than 10%, which is mainly due to a 30% increase in the excited state calculation. But compared to the large computational cost of nonadiabatic couplings, this increase is relatively small—excited-state CPU time scales linearly with the number of excited states, while nonadiabatic couplings scale quadratically. Even the large computational expense of nonadiabatic couplings can be alleviated by reducing the number of computed couplings between states to a small fraction that are nearby in energy to the occupied state of the system. In this way, numerical costs of nonadiabatic couplings become practically independent of the number of excited states.

4. CONCLUSIONS

Modeling solvation has obvious computational challenges due to the number of degrees of freedom in a solvent. Reducing the computational cost needed to model solvation while still capturing the effective solvent response is a desired attribute of solvated atomistic simulations. In this work, we have implemented and demonstrated the use of an implicit solvent model in the Nonadiabatic EXcited-state Molecular Dynamics (NEXMD) software.

The NEXMD software is an efficient framework for excited state modeling of large molecular systems. The code calculates electronically excited states at the time dependent Hartree–Fock (TD-HF) or configuration interaction with singles (CIS) level combined with a family of optimized semiempirical Hamiltonians. This level of theory, merged with improved surface hopping methodologies for electronic transitions, makes it feasible to simulate the nonadiabatic dynamics of molecules with sizes on the order of hundreds of atoms and for time scales up to tens of picoseconds. This is a signature property of the code enabling the simulation of large molecular systems where more elaborate ab initio approaches would be numerically prohibitive. This work introduced a version of NEXMD based on the semiempirical quantum chemistry (SQM) code from AmberTools, which contains a diverse set of semiempirical Hamiltonians and a linear response conductor-like polarizable continuum model (CPCM).

Benchmarks of solvent effects against a test bed of push–pull (donor–acceptor) PPVO derivatives were meant to both validate the use of this CPCM for future studies seeking to utilize the code and determine the interplay of functionalization and solvent polarity on photoinduced nonadiabatic dynamics. Our results showed that solvation can change dynamic and static properties, where the dependence of solvent polarity is determined by molecular polarization due to chemical substitution. In the case of the \{H, H\} oligomer, many of the calculated properties are less dependent on solvent polarity due to the molecule’s low degree of polarizability. On the other hand, substitution with electron donating and withdrawing groups in \{H, NO₂\} and \{NH₂, NO₂\} change excited state lifetimes, exciton localization, and structural relaxation. For example, we established how functionalization and solvent polarity affect spatial confinement of molecular excitations (Figures 5 and 7) and evolution of structural parameters such as bond length alternation (BLA) (Figure 8). Of the many properties that were analyzed, a few followed the expected trends based on chemical and physical intuition such as stabilization of energy levels (Figure 3) and dependence of excited state dipole moments with solvent polarity (Figure 6).

Others, however, such as changes in excited state lifetimes due to solvent-induced fluctuations in energy gaps (Figure 4), are evidence of the complex behavior that solvation can have on nonradiative relaxation. These results suggest that theoretical interpretations may be altered depending on whether the effects of solvation are strong. With an integrated implicit solvent model, the NEXMD software has further become an appealing framework for realistic modeling of the photoinduced nonadiabatic dynamics in a diverse set of solvated chemical systems.

This work both demonstrates an important extension to NEXMD’s capabilities and sets the stage for other advanced features of the code. We have shown that CPCM modeling adds little numerical overhead to the simulations, thus presenting an efficient way to model solvent effects in extended systems. Our future work will include implementation of state-specific and nonequilibrium solvent models in the context of nonadiabatic dynamics. The use of these models is relevant since the dynamics following photoexcitation proceeds through many excited states and are generally out of equilibrium (i.e., the solute and solvent polarizations are not equilibrated with one another). However, more work is needed to determine how important such effects are on dynamics as they likely depend on the solute—solvent system of interest. Furthermore, an important property of the solvent model used for this study is that the coefficient of induced polarization goes as \((\varepsilon - 1)/\varepsilon\); solvent effects asymptotically decrease with increasing \(\varepsilon\) as evidenced by the relaxation time scales of Figure 4D. Whether high dielectric constants significantly change dynamics requires further investigation, which is why extending this work to explicit solvation is important. Indeed there has been an ongoing effort to introduce a QM/MM solvent model to NEXMD, as implemented in AmberTools. The goal is to evaluate implicit and explicit solvation on dynamics, and to assess the validity of each model based on chemical composition of the solute—solvent system.

**ASSOCIATED CONTENT**

**Supporting Information**

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jctc.8b00103.

Detailed description of nonadiabatic dynamics modeling procedure. Comparison of theoretical and experimental optical absorption and emission spectra. NTOs of the first excited state (\(S_1\)) and the optically excited states at 4.30 eV. Energy gaps throughout the dynamics. Number of small energy gaps that fell below a 0.1 eV threshold throughout the dynamics. Exponential rate and time decay constants of fitted \(S_1\) populations (Figure 4). Fraction of TD due to ground to excited state transitions as a function of individual excited states and \(\varepsilon\). Excited state dipole moments as a function of time. Difference of dipole moments in the ground and excited states \(\vec{\mu}_g - \vec{\mu}_e\) as a function of individual excited states and \(\varepsilon\). Solvent-stable resonance structures (zwitterions). Relative CPU times of the nonadiabatic simulations. Comparison between semiempirical theory and TD-DFT for absorption spectra and ground and first excited state dipole moments (PDF)
**AUTHOR INFORMATION**

Corresponding Author  
*E-mail: sergo@lanl.gov*

**ORCID**

Andrew E. Sifain: 0000-0002-2964-1923  
Josiah A. Bjorgaard: 0000-0003-3679-2487  
Tammie R. Nelson: 0000-0001-3773-5291  
Brendan J. Gifford: 0000-0002-4116-711X  
Oleg V. Prezhdo: 0000-0002-5140-5069  
Sebastian Fernandez-Alberti: 0000-0003-3693-8784  
Adrian E. Roitberg: 0000-0001-5547-3647

**Funding**

The authors acknowledge support of the U.S. Department of Energy through the Los Alamos National Laboratory (LANL) LDRD Program. O.V.P. and A.E.S. acknowledge support of the U.S. Department of Energy, Grant DE-SC0014429.

**Notes**

The authors declare no competing financial interest.

**ACKNOWLEDGMENTS**

LANL is operated by Los Alamos National Security, LLC, for the National Nuclear Security Administration of the U.S. Department of Energy under Contract No. DE-AC52-06NA25396. This work was done in part at the Center for Nonlinear Studies (CNLS) and the Center for Integrated Nanotechnologies (CINT) at LANL. We also acknowledge the LANL Institutional Computing (IC) program for providing computational resources. A.E.S. thanks CNLS for their support and hospitality.

**REFERENCES**


DOI: 10.1021/acs.jctc.8b00103

(54) Thouless, D. J. The Quantum Mechanics of Many-Body Systems; Courier Corp.: 2013.


